Forecasting electricity rates via EViews incorporating political decisions

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(4月) (日) (日)

1 Introduction

- Basic Market Structure
- Economic Relevance

2 Modelling electricity rates

3 Forecasting future electricity rates: Approach II

- The Economic Model of Supply and Demand
- Explict Price Equation
- Toy Model
- Literature

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"Die Energie kann als Ursache für alle Veränderungen in der Welt angesehen werden", Werner Heisenberg, Physik und Philosophie

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Main Concerns

Items to address:

• Modelling electricity rates: Key features of the electricity market

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- Modelling electricity rates: Key features of the electricity market
- Electricity rates and EViews: Statistical Inference

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Main Concerns

Items to address:

- Modelling electricity rates: Key features of the electricity market
- Electricity rates and EViews: Statistical Inference
- Stochastic supply and demand: Modelling electricity rates

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First thoughts

Basic Market Structure Economic Relevance

People are interested in energy: Why?

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Basic Market Structure Economic Relevance

First thoughts

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$$E = m * c^2$$

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Basic Market Structure Economic Relevance

First thoughts

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Basic Market Structure Economic Relevance

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- The importance of energy drinks

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Basic Market Structure Economic Relevance

First thoughts

People are interested in energy: Why?

- $E = m * c^2$ maybe but only a few
- The importance of energy drinks probably not
- Energy capacities are bounded

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Basic Market Structure Economic Relevance

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People are interested in energy: Why?

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Basic Market Structu Economic Relevance

First thoughts

People are interested in energy: Why?

- $E = m * c^2$ maybe but only a few
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- Energy capacities are bounded seems true

 $\mathsf{Limited \ capacities} \Rightarrow \mathsf{Access \ restricted}$

 \Rightarrow Energy has a price

Here: Focus on electricity rates

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Basic Market Structure Economic Relevance

Can we model the price?

Energy Law in Germany: Two Landmarks

• till 1998: Energiewirtschaftsgesetz (1935): prevent competition due to "Demarkationsverträge"

 \implies locally monopolistic structure

 \implies Price determined by "individual proposal"

Impossible to provide a "good model"

- from 1998: Gesetz zur Neuregelung des Energiewirtschaftsrechts: Liberalization of electricity market from 2005 onwards
 - \implies Competition

Existence of a market allows for modelling the electricity rates

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Basic Market Structure Economic Relevance

Should we model the price?

• Customer: Agree on prices in advance

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Basic Market Structure Economic Relevance

Should we model the price?

• Customer: Agree on prices in advance \implies No need for modelling the price?

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Basic Market Structure Economic Relevance

Should we model the price?

- Customer: Agree on prices in advance ⇒ No need for modelling the price?
- Energy Suppliers, Electricity Traders: Have to buy electricity on a regular basis
- \implies We should model the price for electricity

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Basic Market Structure Economic Relevance

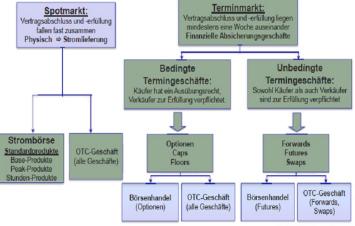
Buy 'the' electricity for 'that' price

Where to buy electricity:

- EEX in Leipzig (Stock Exchange)
- OTC trading

"The" price: Net price (without tax load, grid charges etc.)

Basic Market Structure Economic Relevance



Quelle: Praxisbuch Energiewirtschaft

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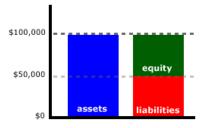
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Economic Relevance I: Balance Sheet of an Energy Supplier

Legal requirements: Since 1998

• KonTraG (Gesetz zur Kontrolle und Transparenz im Unternehmensbereich):

Companies are obliged to disclose their risk profile



Equity = the difference between total assets and total liabilities

Economic Relevance II

- Assets: Future Payments of Energy Consumer
- Liabilities: Suppliers have to buy electricity to meet their contract obligation - Two possibilities
 Spot market: Buy energy in future at spot market non-hedged risk
 Derivative market: Ensure to be able to buy energy in the future for a certain price which does not depend on the market developments - hedged risk

Amount of Liabilities depend on future electricity prices



Basic Market Structure Economic Relevance

A good model for electricity rate propagation will be of key importance

- Improve corporate risk control (reduce risk capital)
- Meet increasing legal requirements

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Electricity Rates

Let's have a look at real data from the EEX: A very short introduction using EViews

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How to find a model for electricity prices?

Essentially two approaches:

- First approach: Apply existing models to the situation at hand and take the one with the best fit.
- Investigate the problem and get a deeper understanding of the price-determining factors

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First Approach

Discriptive and inference statistics with EViews:

- Visualize the Data
- Fit a model
- Forecast

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So far, we have seen that

- Statistic Software can help you to visualize the data
- Statistic Software allows for statistical inference

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Modelling electricity rates	Toy Model
Forecasting future electricity rates: Approach II	Literature



Find a good model

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The Economic Model of Supply and Demand Explict Price Equation Toy Model Literature

Supply and Demand

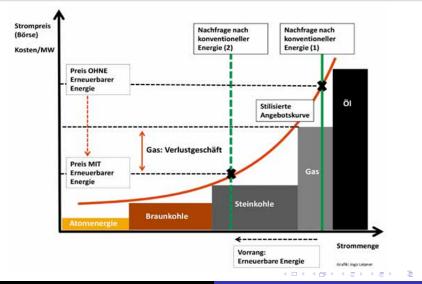
Fundamental economic principle: Supply and Demand

- Demand Curve: Price inelastic (as long as prices remain positive)
 Predictable (small volatility)
- Supply Curve: Merit Order Rule (next slide) ⇒ Supply Curve is price elastic

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Merit Order Rule



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Erneuerbare Energien Gesetz (EEG)

EEG: Renewable energy will be at first fed into the grid Implies Supply Curve with high volatility depending on

- Solar radiation
- Wind force and wind direction

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The price equation

Definition

Energy price=costs for the finally generated KWh

Theorem

The price is determined by the following formular:

$$P_t = \min(p_t(j) : j = \min\{u : f_t(u) := \sum_{i=1}^u S_t(i) \ge D_t\}, \quad (1)$$

 $S_t(i) =$ amount of electricity generated by unit *i*. $D_t =$ electricity demand at time *t*. $p_t(j) =$ unit *j*'s cost for producing one kWh.

Observation: P_t is in general not a continuous variable

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Demand Curve:

$$D(P) = \begin{cases} D^{1}(P) & P \leq 0\\ D^{0} & P \geq 0 \text{ no price sensitivity} \end{cases}$$
(2)

Supply Curve:

$$S(P) = \begin{cases} S^0 & P \le 0 \text{ no price sensitivity} \\ S^1(P) & P \ge 0 \end{cases}$$
(3)

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Toy Example

Demand and Supply Curve with continuous paths: Demand Curve:

$$D(P) = \begin{cases} D_t^0 + \sqrt[\beta]{-P} & P \le 0\\ D_t^0 & P \ge 0 \end{cases}$$
(4)

Supply Curve:

$$S_t(P) = \begin{cases} S_t^0 & P \le 0\\ \sqrt[\alpha]{P} + S_t^0 & P \ge 0 \end{cases}$$
(5)

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Macroeconomic Theorem of Price

Theorem

The observed market price is the price for which

$$S_t(P_0) = D_t(P_0).$$
 (6)

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Plug in (5) and (4) to (6):

$$P(S^0_t, D^0_t) = \left\{egin{array}{cc} -(S^0_t - D^0_t)^eta & D^0_t \leq S^0_t \ (D^0_t - S^0_t)^lpha & D^0_t \geq S^0_t \end{array}
ight.$$

(7)

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Our aim: Understand the mechanism that determines the price. We

- Explained the basic shape of the Demand Curve and the Supply Curve
- Derive an exact formular for the price

So far...

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So far

Our aim: Understand the mechanism that determines the price. We

- Explained the basic shape of the Demand Curve and the Supply Curve
- Derive an exact formular for the price Difficult to apply directly, since S_t(i), D_t and p_t(j) not known
- Use the toy example (continuous paths!) ⇒ Allows to derive an exact formula for the price

The Economic Model of Supply and Demand Explict Price Equation **Toy Model** Literature

Is this a stochastic model?

We have

- Have Supply and Demand Curve
- Intersection yield uniquely determined price P_0

Where is the randomness?

Recall formular for the price:

$$P(S_t^0, D_t^0) = \begin{cases} -(S_t^0 - D_t^0)^{\beta} & D_t^0 \le S_t^0 \\ (D_t^0 - S_t^0)^{\alpha} & D_t^0 \ge S_t^0 \end{cases}$$
(8)

The Economic Model of Supply and Demand Explict Price Equation **Toy Model** Literature

Minimal Supply and Demand

Up to now: No definition of S_t^0

- Recall D⁰_t: Electricity demand depending on t (constant in P for P₀ > 0)
- S_t^0 = Minmial amount of energy feed into the grid (solar energy, wind energy, nuclear power etc.)

Amount cannot be determined in advance for

- Solar Energy
- Wind Energy

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Toy Example II

Supply and Demand as Stochastic Processes

$$dD_t^0 = MeanReversion_D * (D_t^0 - NormalLevel_t)dt + \sigma dW_t.$$
 (9)

$$dS_t^0 = MeanReversion_S * (S_t^0 - NormalLevel_t)dt +
ho dB_t.$$
 (10)

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The Economic Model of Supply and Demand Explict Price Equation **Toy Model** Literature

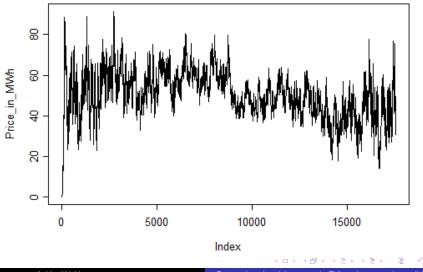
Toy Model II: Simulating Supply and Demand

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Toy Model III: The derived Price Curve



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Final Conclusions

Two approaches for modelling electricity

- Approach I: Calibrate existing models to the data
- Approach II: Develop a new model for electricity

We have seen

- There is an explicit stochastic formula for the price, but not all parameters are known!
- \implies Toy model: explicit model for Supply and Demand
- Results: Merit Order together with EEG will increase volatility in the market
- But where are political decisions incorporated in the model?

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Thank you for your Attention

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